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Kjerneregelen

Oppgave 1

Finn $f'(x)$ til følgende funksjoner:

$$\text{a) } f(x) = (x^3 + 6x)^5 \quad \text{b) } f(x) = \sqrt{2x^2 + 5} \quad \text{c) } f(x) = \left(\frac{2x}{x^2 + 3}\right)^4$$

$$\text{d) } f(x) = (2x^4 + 9)^{3/2} \quad \text{e) } f(x) = \frac{1}{\sqrt{1 + x^2}} \quad \text{f) } f(x) = x^2 \cdot (x^2 + 2x)^3$$

$$\text{g) } f(x) = x^2 \cdot \sqrt{x^2 - 2x} \quad \text{h) } f(x) = \frac{x^2}{(x^2 + x)^3} \quad \text{i) } f(x) = (x^2 + 1)^2 \cdot (x^3 + 1)^3$$

Oppgave 2

Deriver funksjonene nedenfor.

$$\text{a) } f(x) = \sqrt{(3x^2 + 2x)^4} \quad \text{b) } f(x) = (x^3 + 3)^5 \cdot (x^2 + 3)^4 \quad \text{c) } f(x) = \sqrt{x^2 + 1} \cdot x^2$$

$$\text{d) } f(x) = \frac{(2x + 3x^2)^3}{x^2} \quad \text{e) } f(x) = \sqrt[3]{x^4 - 5} \quad \text{f) } f(x) = \frac{x^3}{\sqrt{x^4 - 1}}$$